

Enrollment No./Seat No.:

GUJARAT TECHNOLOGICAL UNIVERSITY

Bachelor of Engineering - SEMESTER - 1/2 EXAMINATION - WINTER 2025

Subject Code: 3110019

Date: 31-12-2025

Subject Name: Remedial Mathematics

Time: 02:30 PM TO 05:00 PM

Total Marks: 70

Instructions

2. Make suitable assumptions wherever necessary.

3. Figures to the right indicate full marks.

	Marks
Q.1 (a) Define slope of a line and find the slope of the line joining the points (2, 3) and (−1, 5).	03
(b) Find the equation of a line passing through (2, −3) and perpendicular to the line $3x - 4y + 7 = 0$.	04
(c) Find the distance of the point (4, −3) from the line $3x + 4y - 5 = 0$.	07
Q.2 (a) Define real-valued function with examples.	03
(b) Express $\sin 3x$ and $\cos 3x$.	04
(c) Prove $\sin(x+y)\sin(x-y) = \sin^2 x - \sin^2 y$.	07
OR	
(c) Find $\lim_{x \rightarrow 0} \frac{\sin 3x}{x}$ Also Define limits and continuity of function	07
Q.3 (a) Check continuity of $f(x) = x^2$ ($x < 1$), $3x - 2$ ($x \geq 1$) at $x = 1$.	03
(b) If $y = x^2 \sin x$, find dy/dx and d^2y/dx^2 .	04
(c) Differentiate the function $\frac{\sin(3x + 5)}{\cos x}$	07
OR	
(a) Find $\int (\sin x + \cos 2x) dx$	03
(b) Find $\int_1^2 (4X^3 - 5X^2 + 6X + 9) dX$	04
(c) Integrate the function $\frac{x}{(x + 1)(x + 2)} dx$	07
Q.4 (a) Find the transpose of the given matrix $\begin{pmatrix} 1 & 2 \\ 0 & 8 \end{pmatrix}$	03
(b) Write Minors and Cofactors of the determinant $\begin{vmatrix} 2 & -4 \\ 0 & 3 \end{vmatrix}$	04

- (c) Find the inverse of the matrix

07

$$\begin{pmatrix} 1 & 2 & 3 \\ 0 & 2 & 4 \\ 0 & 0 & 5 \end{pmatrix}$$

OR

- (a) Compute the products

03

$$\begin{bmatrix} 1 & -2 \\ 2 & 3 \end{bmatrix} \begin{pmatrix} 1 & 2 & 3 \\ 2 & 3 & 1 \end{pmatrix}$$

- (b) If A and B are symmetric matrices, prove that AB - BA is a skew symmetric matrix

04

- (c) Solve system of linear equation, using matrix method : $4x - 3y = 3$ and $3x - 5y = 7$

07

Q.5 (a)

03

The degree of the differential equation 1) $y'' + \sin x - 5 = 0$ 2) $\frac{dy}{dx} = \sin(2x - 8)$

- (b)

04

Find the solution of the differential equation $x^5 \frac{dy}{dx} = -y^5$

- (c)

07

Find a particular solution of the differential equation $\frac{dy}{dx} + y \cot x = 4x \operatorname{cosec} x$ given that $y = 0$ when $x = 0$

OR

- (a) $y = x^2 + 2x + c$ is solution of $y' - 2x - 2 = 0$?

03

- (b)

04

Find the particular solution of the : $x(x^2 - 1) \frac{dy}{dx} = 1; y = 0, x = 2$

- (c)

07

Find the solution of the $\frac{dy}{dx} + 2y \tan x = \sin x$ when $y = 0, x = 0$
