

GUJARAT TECHNOLOGICAL UNIVERSITY**Bachelor of Engineering - SEMESTER - III EXAMINATION - WINTER 2025****Subject Code: 2130002****Date: 29-12-2025****Subject Name: Advance Engineering Mathematics****Time: 10:30 AM TO 01:30 PM****Total Marks: 70****Instructions**

- 1. Attempt all questions.**
- 2. Make suitable assumptions wherever necessary.**
- 3. Figures to the right indicate full marks.**
- 4. Simple and non-programmable scientific calculators are allowed.**

	Marks
Q.1 (a) Define Signum function, Dirac's Delta function and Beta function.	03
(b) Solve $\frac{d^3y}{dx^3} + \frac{dy}{dx} = \operatorname{cosec} x$ by method of variation of parameter.	04
(c) Obtain the Fourier series of $f(x) = \left(\frac{\pi - x}{2}\right)^2$ in the interval $0 \leq x \leq 2\pi$. Hence deduce that $\frac{\pi^2}{12} = \frac{1}{1^2} - \frac{1}{2^2} + \frac{1}{3^2} - \dots$	07
Q.2 (a) Find half range cosine series for $f(x) = x, 0 < x < 3$	03
(b) Solve $\frac{d^3y}{dx^3} - \frac{d^2y}{dx^2} + 3\frac{dy}{dx} + 5y = e^x \cos 3x$	04
(c) Find the series solution of $y'' = 2y'$ in powers of x	07
OR	
(c) Find the series solution of $(1 + x^2)y'' + xy' - xy = 0$	07
Q.3 (a) Solve $\frac{dy}{dx} + 2y \tan x = \sin x$	03
(b) Solve $(x^3 + 3xy^2)dx + (3x^2y + y^3)dy = 0$	04
(c) Solve $(D^3 - D^2 - 6D)y = x^2 + 1$	07
OR	
(a) Solve $\frac{dy}{dx} + \frac{y \cos x + \sin y + y}{\sin x + x \cos y + x} = 0$	03
(b) Solve $(x^2y^2 + 2)ydx + (2 - x^2y^2)xdy = 0$	04
(c) Solve $(D^4 + 2D^3 - 3D^2)y = x^2 + 3e^{2x}$	07

- Q.4 (a)** Find the Laplace Transform of $e^{-2t}(\sin 4t + t^2)$ **03**
- (b)** **04**
Find the Inverse Laplace Transform of $\log \left(1 + \frac{\omega^2}{s^2} \right)$
- (c)** **07**
Find the Inverse Laplace transform of $\frac{5s + 3}{(s - 1)(s^2 + 2s + 5)}$ using partial fraction.

OR

- (a)** Find the Laplace Transform of $\sin 2t \cdot \sin 3t$ **03**
- (b)** Find the Laplace Transform of $t^2 \cosh \pi t$ **04**
- (c)** **07**
Solve the initial value problem $\frac{d^2x}{dt^2} + 2\frac{dx}{dt} + 5x = e^{-t} \sin t$ where $x(0) = 0$ and $x'(0) = 1$ using Laplace transform.
- Q.5 (a)** Form a partial differential equation by eliminating the arbitrary constants for the equation $z = (x - 2)^2 + (y - 3)^2$ **03**
- (b)** Solve $pz - qz = z^2 + (x + y)^2$ using Lagrange's method **04**
- (c)** **07**
Solve $\frac{\partial^2 z}{\partial x^2} - 2\frac{\partial z}{\partial x} + \frac{\partial z}{\partial y} = 0$ using method of separation of variables.

OR

- (a)** Solve $p(1 + q) = qz$ **03**
- (b)** **04**
Solve the below equation by method of direct integration, $\frac{\partial^2 z}{\partial x \partial y} = \sin x \sin y$, given
that $\frac{\partial z}{\partial y} = -2 \sin y$ when $x = 0$ and $z = 0$ when y is an odd multiple of $\frac{\pi}{2}$
- (c)** **07**
Solve $\frac{\partial u}{\partial x} + \frac{\partial u}{\partial y} = 2(x + y)u$ using method of separation of variables.
